



Calculations Policy
Addition and Subtraction

Addition

5 Counting Principles (Early Years) :

1. The one-one principle.

- Children assign one number name to each object that is being counted.
- Children must ensure that they count each object only once.



1



2



3



4



5

2. The stable-order principle

- Children understand that, when counting, the numbers have to be said in a certain order.

3. The cardinal principle

- Children understand that the number name assigned to the final object in the group is the total number of objects in that group.

4. The abstraction principle

- Children understand that anything can be counted, including things that cannot be touched eg. Sounds and movements

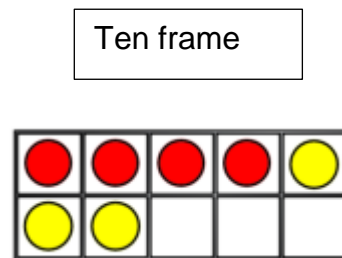
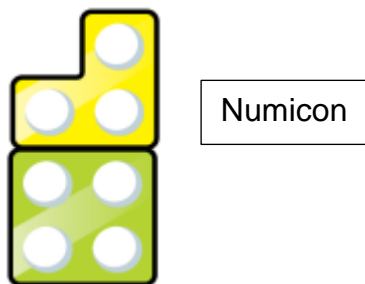
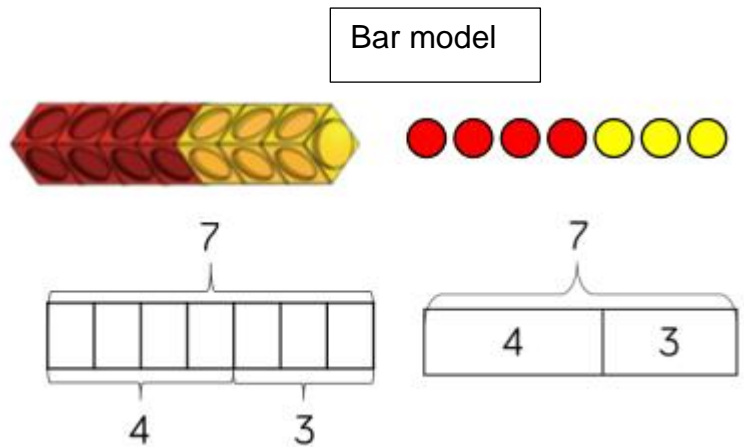
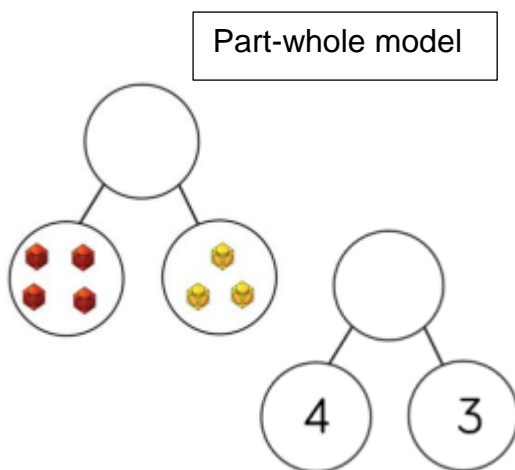
5. The order-irrelevance principle

- Children understand that whatever order we count a group of objects in, there will still be the same number.

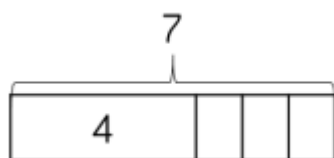
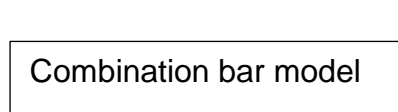
Add two 1-digit numbers to 10 (Early Years and Year 1)

When adding numbers to 10, children can explore both aggregation and augmentation.

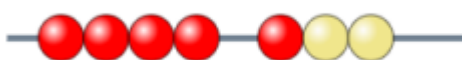
Models to support aggregation:



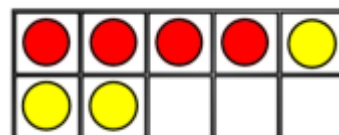
Models to support augmentation:



Bead string



Ten frame



Number track



Add 1 and 2-digit numbers to 20 (Year 1 and 2)

The knowledge that 10 ones equal 1 ten supports children in adding 1-digit numbers that cross 10.

In Year 1 this is done by counting on using the following models to support:

The image shows three models for the addition $8 + 7 = 15$:

- Part-whole model:** A large circle is divided into two smaller circles. The top circle contains the number 7, and the bottom circle contains the number 8.
- Bar model:** A horizontal bar is divided into two sections. The left section is labeled 8 and the right section is labeled 7. A bracket above the entire bar is labeled 15.
- Numicon:** Two vertical rods. The left rod is blue and has 8 dots (4 on top, 4 on bottom). The right rod is pink and has 7 dots (3 on top, 4 on bottom).

Labels: Part-whole model, Bar model, Numicon

In Year 2, different manipulatives can be used to represent the exchanging of ten 1s for one 10 alongside number lines to support children in understanding how to partition their jumps:

The image shows three models for the addition $8 + 7 = 15$ in Year 2:

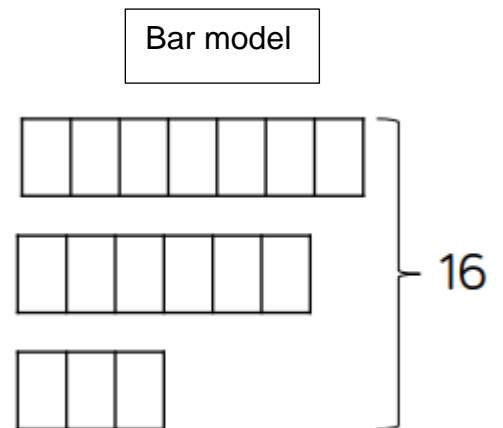
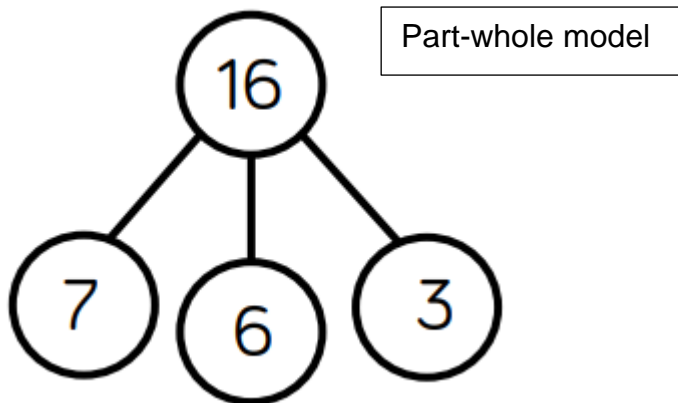
- Straws bundles to make 10:** Two rows of 10 straws each. An arrow points down to a bundle of 10 straws and 5 individual straws.
- Ten frame filled to make 10:** Two ten frames. The first frame has 8 red dots and 2 yellow dots. The second frame has 7 red dots and 5 yellow dots.
- Number line:** A number line from 0 to 20. A blue oval highlights the equation $8 + 7 = 15$ with a bracket under 2 and 5. Below the line, a blue arrow jumps from 8 to 10 (+2), and another blue arrow jumps from 10 to 15 (+5).

Labels: Straws bundles to make 10, Ten frame filled to make 10, Number line

Add three 1-digit numbers (Year 2)

When adding three 1-digit numbers, children should be encouraged to look for number bonds to 10 or doubles to add more efficiently. This also supports their understanding of commutativity.

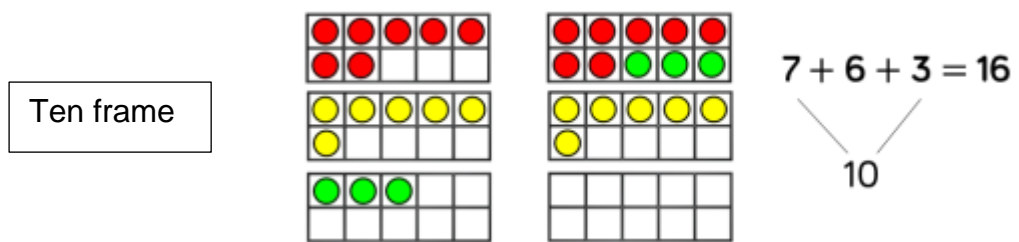
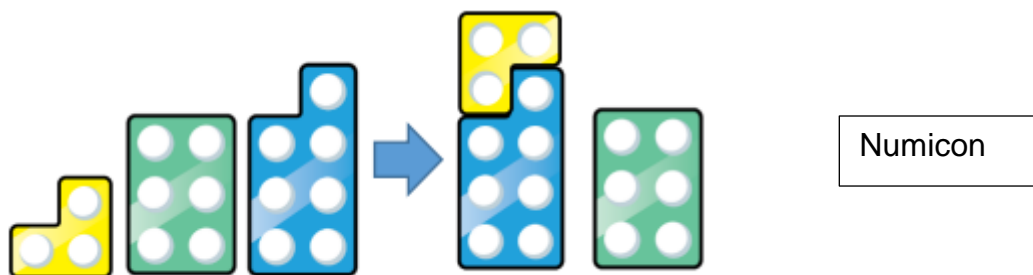
The following representations may be used:



$7 + 6 + 3 = 16$

Abstract

Representations that highlight number bonds to 10 are effective when adding three 1-digit numbers:



Add 1-digit and 2-digit numbers to 100 (Year 2 and 3)

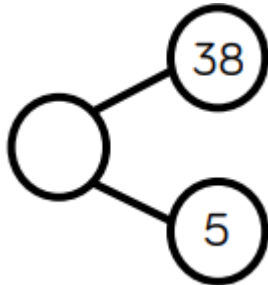
When adding 1-digit to a 2-digit number, children should be encouraged to count on from the larger number.

They should apply their knowledge of number bonds to add more efficiently

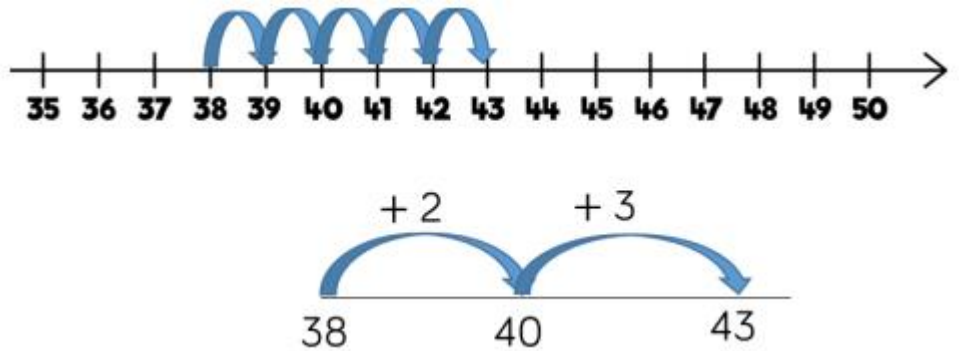
eg. $8 + 5 = 13$ so $38 + 5 = 43$

The following representations may be used (hundred squares and straws help children to find the number bond to 10):

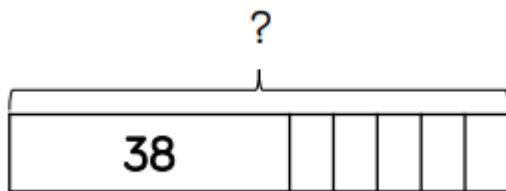
Part-whole model



Numberlines

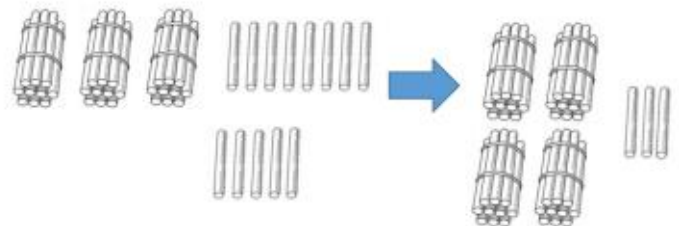


Bar model



$$38 + 5 = 43$$

Abstract



Straws

Hundred square

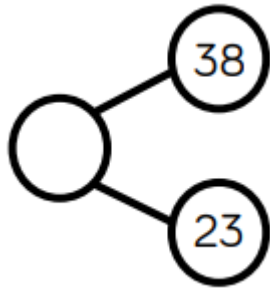
1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100

Add 2-digit numbers to 100 (Year 2 and 3)

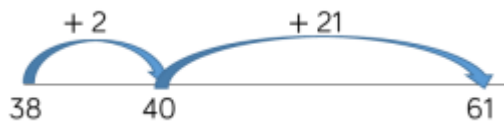
Children can count on to find the total. They should be encouraged to jump to multiples of 10 to be more efficient.

The following representations may be used:

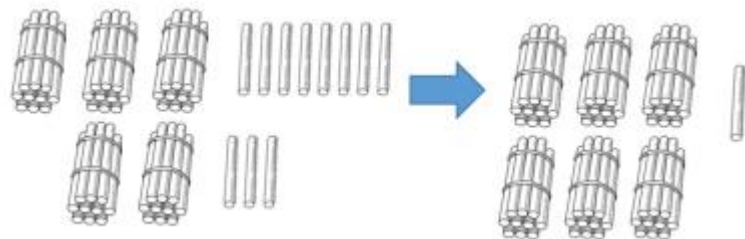
Part-whole model



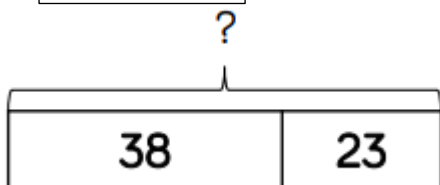
Numberline



Straws



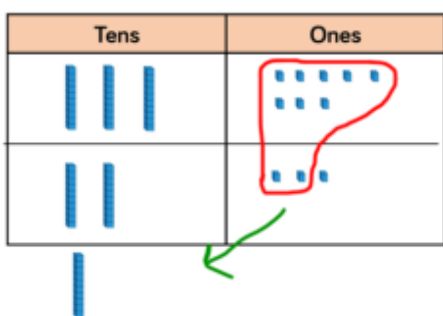
Bar model



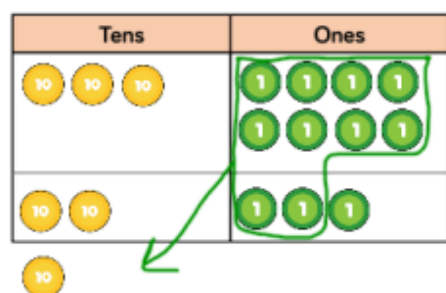
Abstract

$$38 + 23 = 61$$

From year 3, children should be encouraged to use the formal column method, firstly calculating alongside base ten or place value counters:



$$\begin{array}{r} 38 \\ + 23 \\ \hline 61 \\ 1 \end{array}$$

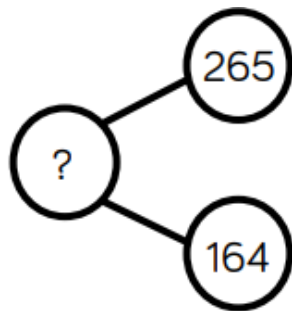


Add numbers with up to 3 digits (year 3)

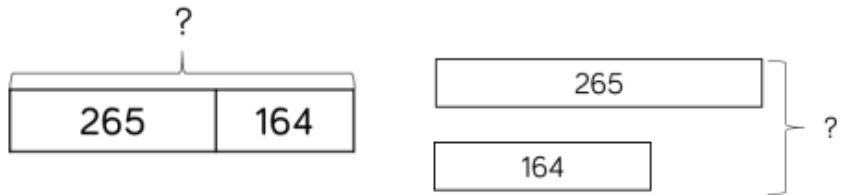
Children should write their calculation alongside any concrete resources so that they can make links to the written column method.

The following representations may be used to support:

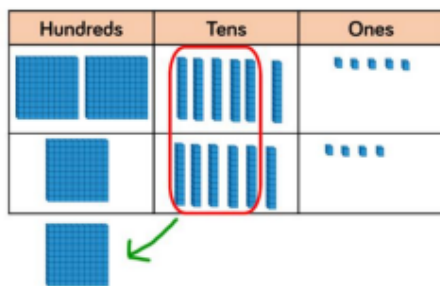
Part-whole model



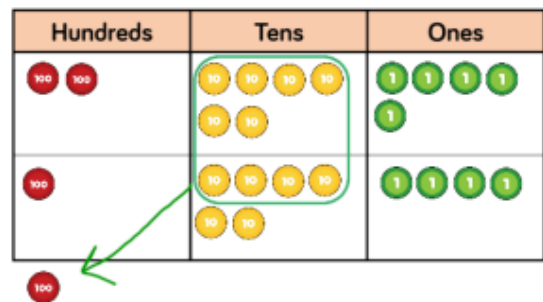
Bar models



Base ten and place value counters alongside formal column method



$$\begin{array}{r} 265 \\ + 164 \\ \hline 429 \\ \hline 1 \end{array}$$

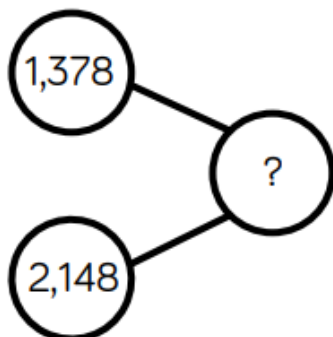


Add numbers with up to 4 digits (Year 4)

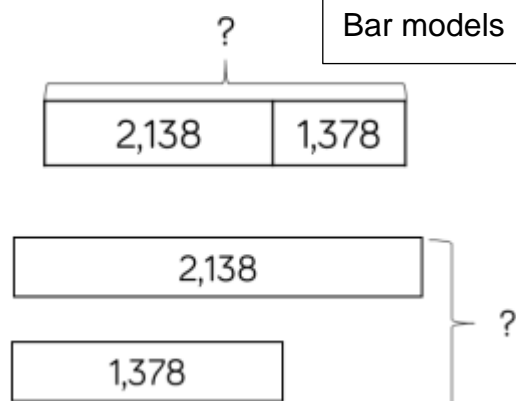
Children should write their calculation alongside any concrete resources so that they can make links to the written column method.

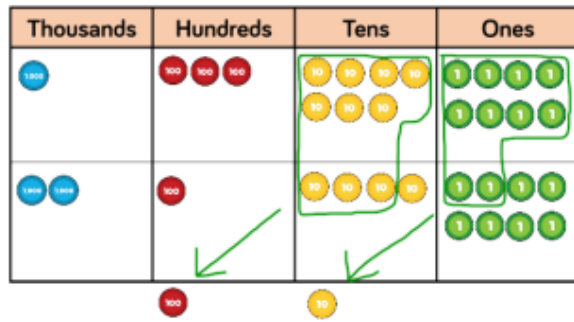
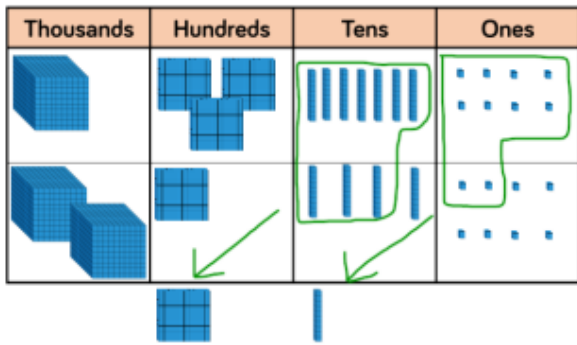
The following representations may be used to support:

Part-whole model



Bar models





Base ten and place value counters alongside formal column method

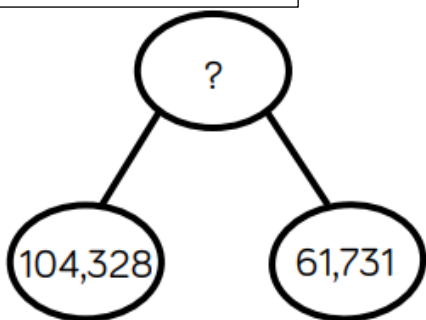
	1	3	7	8
+	2	1	4	8
	3	5	2	6
		1	1	

Add numbers with more than 4 digits (Year 5 and 6)

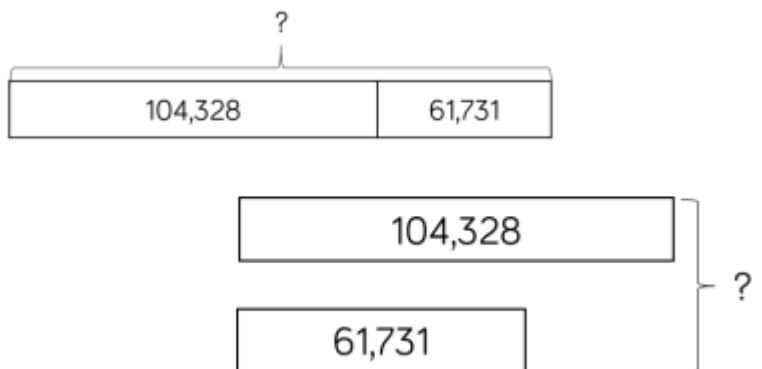
Children should be encouraged to work in the abstract, using the column method to add larger numbers efficiently. However, place value counters on a place value grid may support understanding.

The following representations may be used:

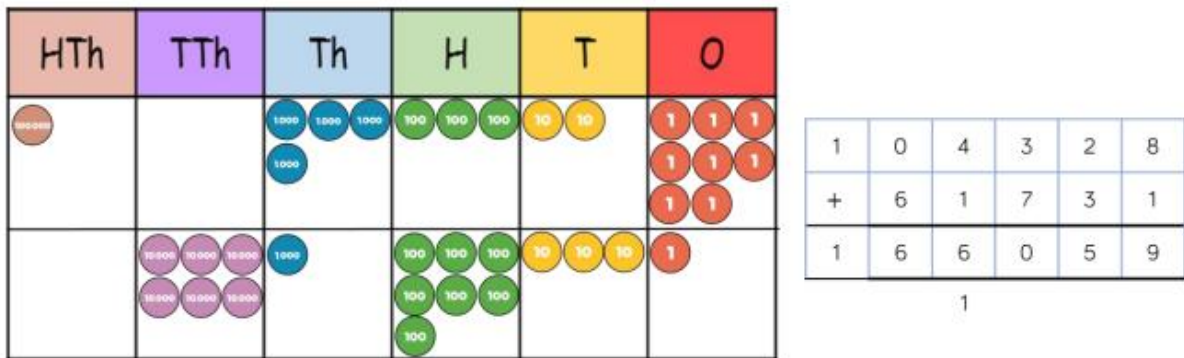
Part-whole model



Bar models



Place value counters on a place value chart alongside formal column method

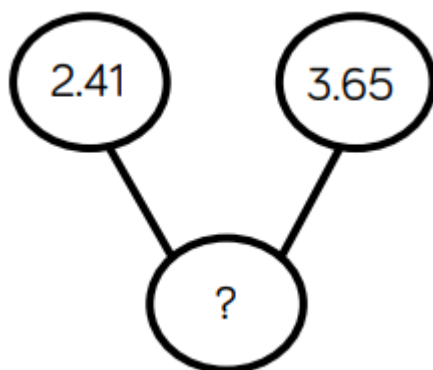


Add numbers with up to 3 decimal places (Year 5)

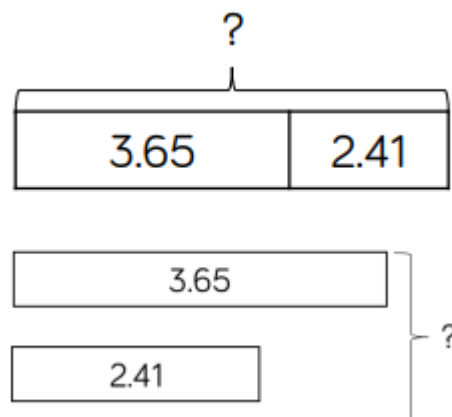
Children should have experience of adding decimals with a variety of decimal places. This should also be put into context when adding money and other measures.

The following representations may be used:

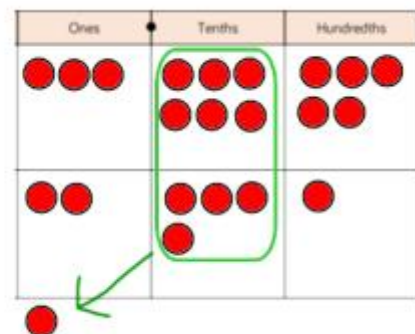
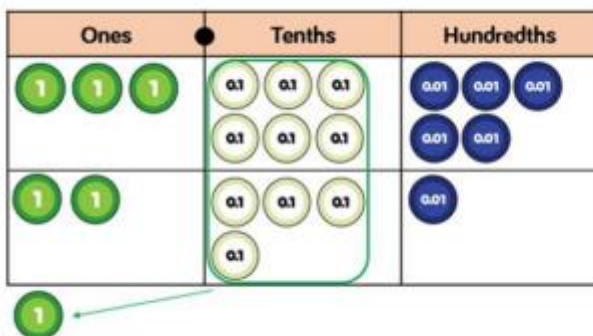
Part-whole model



Bar models



Place value counters or plain counters on a place value chart



$$\begin{array}{r} 3.65 \\ + 2.41 \\ \hline 6.06 \\ \hline 1 \end{array}$$

Abstract

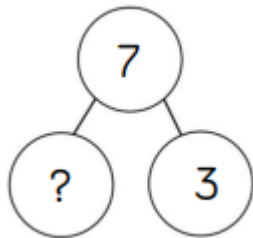
Subtraction

Subtract 1-digit numbers within 10 (Early Years and Year 1)

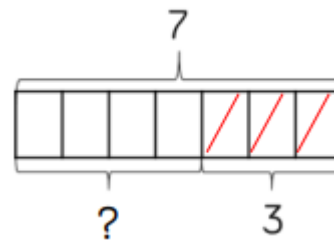
1-digit numbers within 10 can be subtracted using partitioning, reduction and finding the difference.

The following representations support partitioning:

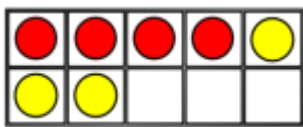
Part-whole model



Bar models

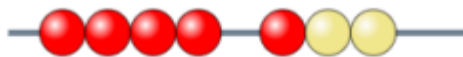


Ten frame



Numicon

The following representations support reduction:

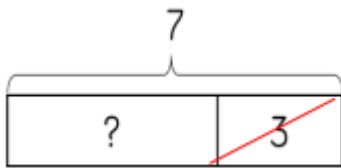


Bead strings

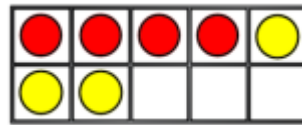


Number tracks

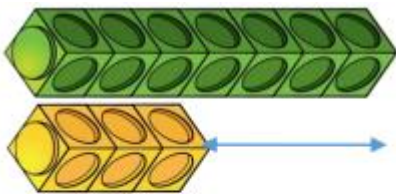
Single bar models



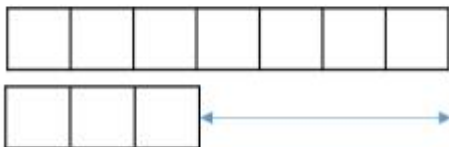
Ten frame



The following representations support finding the difference:



Cubes



Bar models with two bars

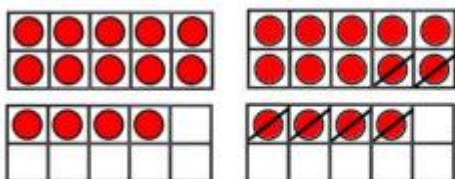
Subtract 1 and 2-digit numbers to 20 (year 1 and 2)

When subtracting 1-digit numbers that cross 10, it is important to highlight the importance of ten 1s equalling one 10.

Children should be encouraged to find the number bond to 10 when partitioning the subtracted number.

The following representations are particularly useful for this alongside the abstract:

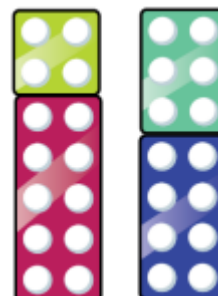
Ten frames



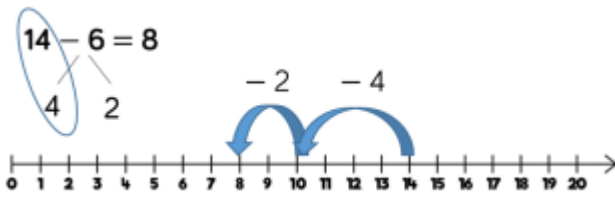
Numicon

$$14 - 6 = 8$$

The number 14 is circled. A line connects the 4 to the 6, and another line connects the 2 to the 6, illustrating the partitioning of 6 into 4 and 2.

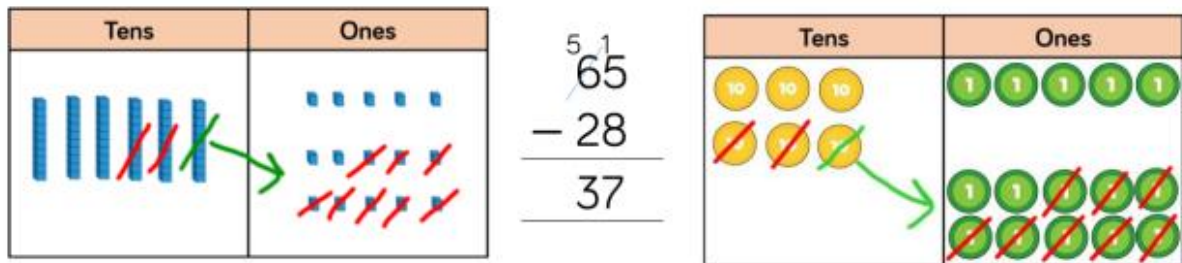


Number lines

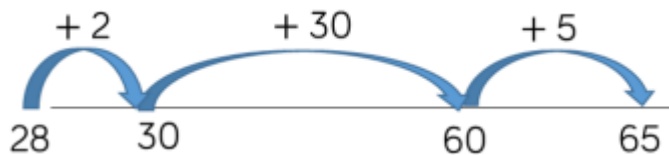


Subtract 1 and 2 digit numbers to 100 (year 2)

At this stage, children should be encouraged to use the formal column method alongside base ten and place value counters.

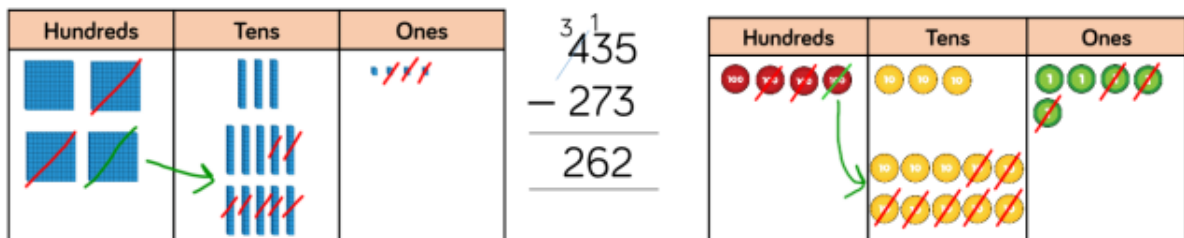


Children can also use a blank number line to count on to find the difference. They should be encouraged to jump to multiples of 10 to work efficiently.

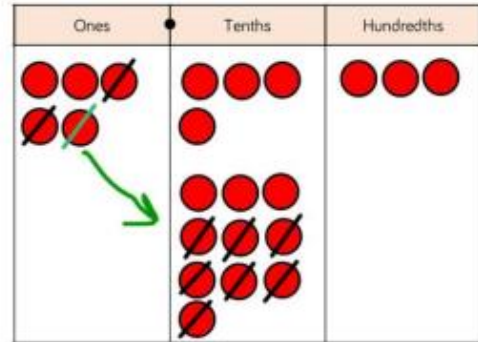
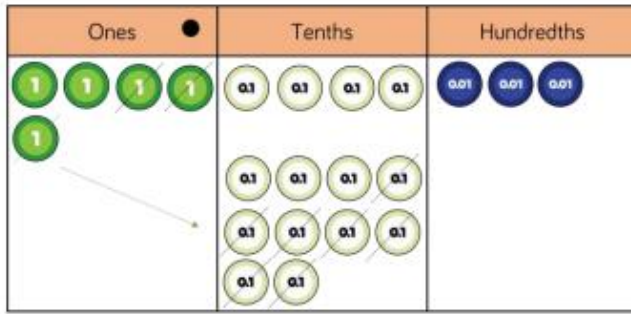


Subtract numbers with up to 3 digits (year 3)

Children should be encouraged to write out any calculations in a formal column method alongside the use of manipulatives so that they can make links between the two.



Place value counters or plain counters on a place value chart may support a written column method.



$$\begin{array}{r}
 ^4 ^1 \\
 5.43 \\
 - 2.7 \\
 \hline
 2.73
 \end{array}$$

Glossary:

Addend: A number to be added to another

Aggregation: Combining two or more quantities or measures to find a total

Augmentation: Increasing a quantity or measure by another quantity

Commutative: Numbers can be added in any order

Complement: In addition, a number and its complement make a total eg.300 is the complement to 700 to make 1000

Difference: The numerical difference between two numbers is found by comparing the quantity of each group

Exchange: Change a number or expression for another of an equal value

Minuend: A quantity or number from which another is subtracted

Partitioning: Splitting a number into its component parts

Reduction: Subtraction as take away

Subitise: Instantly recognise the number of objects in a small group, without needing to count

Subtrahend: A number to be subtracted from another

Sum: The result of an addition

Total: The aggregate or the sum found by addition